Kondo effect in a one-electron double quantum dot: Oscillations of the Kondo current in a weak magnetic field

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We present transport measurements of the Kondo effect in a double quantum dot charged with only one or two electrons, respectively. For the one-electron case, we observe a surprising quasiperiodic oscillation of the Kondo conductance as a function of a small perpendicular magnetic field \( |B_z| \leq 50 \text{ mT} \). We discuss possible explanations of this effect and interpret it by means of a fine tuning of the energy mismatch of the single dot levels of the two quantum dots. The observed degree of control implies important consequences for applications in quantum information processing.

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The Kondo effect describes a bound state formed by interactions between a localized magnetic impurity and itinerant conduction-band electrons shielding the localized spin. This results in an increased density of localized states at the Fermi energy, causing anomalous low-temperature properties. In the case of a degenerate ground state of a quantum dot (QD), the Kondo effect manifests itself as an enhanced conductance within the Coulomb blockade regime. This was first observed on large QDs with half-integer spin, and later, for a total spin of \( S = 1 \), where the triplet states of a QD are degenerate. On a double quantum dot (DQD), a two-impurity Kondo effect was studied.

In this paper, we present the results of Kondo effect differential conductance (KDC) measurements on a DQD charged with one or two electrons in a perpendicular magnetic field \( B_z \). For only one electron \( (N=1) \) in the DQD, we observe a quasiperiodic structure of the KDC with a characteristic scale of \( B_0 \approx 10 \text{ mT} \). In contrast, for \( N=2 \) the KDC is found to be a monotonous function of \( B_z \). We discuss possible explanations for this effect that imply consequences in quantum information processing.

Our sample is fabricated from an AlGaAs/GaAs heterostructure. It embeds a two-dimensional electron system (2DES) with carrier density \( n_i = 1.8 \times 10^{15} \text{ m}^{-2} \) and electron mobility \( \mu \approx 75 \text{ m}^2/\text{Vs} \) (at \( T=4.2 \text{ K} \) ) 120 nm below its surface. Figure 1(b) shows Ti/Au gates created by electron-beam lithography. They are used to locally deplete the 2DES to define a one-electron QD. The gate design is optimized for transport measurements through a QD charged by only few electrons. By decreasing the voltages applied to gates \( g_C \) and \( g_X \) (with respect to the 2DES) while increasing the voltages on the side gates \( g_L \) and \( g_R \), we deform the QD into a DQD [sketched in Fig. 1(b)]. The DQD is tuned to the regime of strong coupling to the leads and an order of magnitude stronger interdot tunnel coupling of \( 2t_0 \approx 240 \text{ \( \mu \text{eV} \) \} between the adjacent QDs. Measurements are performed in a dilution refrigerator at an electron temperature \( T_{2DES} \approx 0.1 \text{ K} \).

A nearby quantum point contact (QPC) is used to detect the charge distribution of the DQD shown in the stability diagram in Fig. 1(a). It displays a lock-in measurement of the differential transconductance \( G_{\text{QPC}}(U) = dI_{\text{QPC}}/dU_N \) as a function of the dc voltages applied to gates \( g_L \) and \( g_R \). In the lower left corner region in Fig. 1(a), the DQD is uncharged (compare the figure caption).

The differential conductance of the DQD is plotted in Fig. 1(c) as a function of the applied bias voltage \( U_{SD} \) and the center gate voltage \( U_C \). The DQD is tuned such that the variation in \( U_{SC} \) (x axis) causes a shift in the stability diagram approximately along the arrow in Fig. 1(a). Hence, a charge between \( N=0 \) and 3 electrons, marked in Fig. 1(c) by numerals, is distributed symmetrically between the adjacent QDs. Within the diamond-shaped regions transport is impeded by Coulomb blockade (CB). Nevertheless, strong coupling of our DQD to its leads allows for inelastic cotunneling causing an enhanced conductance within the CB regions at \( U_{SD} \neq 0 \), e.g., for \( N=1 \) at \( |eU_{SD}| \approx 2t_0 = 240 \text{ \( \mu \text{eV} \) \}.

In addition, at \( U_{SD} \approx 0 \) an increased differential conductance is visible in the CB regions for \( N=1, 2, \) or 3. We assign this zero-bias anomaly to the Kondo effect on a DQD, here charged with only a few electrons. The observed KDC is small compared to the unitary limit \( (G \approx 2e^2/h) \). This is due to the tunnel barrier hindering electron transport between the two adjacent QDs and to an asymmetric coupling to the leads.

Figure 2 displays the KDC at \( U_{SD} \approx 0 \) of the DQD as a
the KDC at B. For increasing \( T \) tensions with \( \text{a hydrogen path in the stability diagram indicated by an arrow in} \) the limits Pustilnik and Glazman provides analytical expressions for monotonically as the spin degeneracy is lifted. A theory by

\[ G = \mu_B \delta_B \text{ in } G \text{ the KDC of the DQD at } N=2 \text{ as a function of the side gate voltages } U_{g R} \text{ and } U_{g L}. \]

The measurement was done by using a nearby QPC. A background is subtracted for clarity. Numerals denote the number of electrons charging the right surface. Arrows mark possible current paths through the DQD and the nearby QPC. The estimated DQD geometry is sketched in white.

\[ G(\mu_B \delta_B) \text{ of the symmetrically charged DQD as a function of bias voltage } U_{g R} \text{ and center gate voltage } U_{g C}. \]

The variation of \( U_{g C} \) corresponds approximately along the white vertical lines in Fig. 1(c). Three of these traces \( G(U_{g R}) \) are plotted in the inset of Fig. 2. For increasing \( B_{\perp} \), the KDC is expected to decrease monotonically as the spin degeneracy is lifted. A theory by Pustilnik and Glazman provides analytical expressions for the limits \( B \ll B_K \) and \( B \gg B_K \),

\[ (B_{\perp}/B_K)^2 \] for \( B \ll B_K \), the KDC is described by \( G = G_0 \left[ 1 - (B_{\perp}/B_K)^2 \right] \) and for \( B_{\perp} \gg B_K \) by \( G = G_0 \left[ 1 - \ln^2(B_{\perp}/B_K) \right] \).

\( G_0 \) is the KDC at \( B_{\perp} = 0 \). The lines in Fig. 2 model these expressions with \( T_K = 0.1 \text{ K for } N=1 \) and \( T_K = 0.12 \text{ K for } N=2 \). \( T_K \) is taken identical for both limits (solid and dashed lines), respectively. Being close to the electron temperature of the 2DES, \( T_K \) cannot be extracted from temperature dependences as usual. Nevertheless, the model curves used here are expected to hold even for \( T_K \approx T_{2\text{DES}} \). The agreement with our data is satisfactory.

For \( B_{\perp} \approx 0.5 \text{ T} \), the decrease of the KDC gets steeper due to a \( B_{\perp} \)-dependent decrease of the interdot tunnel coupling, specifically investigated for our DQD. Taking such effects into account does not change the Kondo temperature too much compared to the simple model presented here. However, our simplified model causes the fit-parameter \( G_0 \) to be strongly suppressed compared to \( G_0 \).

Figure 3 shows detailed measurements of the KDC for

\[ T_K \text{ and } \delta_B \text{ in the main figure display the KDC in a logarithmic scale at } U_{g R} = 0 \text{ (local maxima of raw data curves) as a function of a perpendicular magnetic field. Lines are model curves explained in the main text.} \]

\[ G(\mu_B \delta_B) = \text{ model for } B \ll B_K \]

\[ G(\mu_B \delta_B) = \text{ model for } B \gg B_K \]

\[ G(\mu_B \delta_B) = \text{ model for } B_{\perp} \approx B_K \]

\[ G(\mu_B \delta_B) = \text{ model for } B \approx B_K \]

FIG. 2. Kondo effect differential conductance in a one- (two-) electron DQD. The inset displays exemplary raw data curves of the KDC of the DQD at \( N=2 \) as a function of the bias voltage for different magnetic fields but constant gate voltages. All raw data curves are measured within CB regions as sketched by the vertical white lines in Fig. 1. Black \( (N=1) \) and gray \( (N=2) \) circles in the main figure display the KDC in a logarithmic scale at \( U_{g R} = 0 \) (local maxima of raw data curves) as a function of a perpendicular magnetic field. Lines are model curves explained in the main text.

FIG. 3. Nonmonotonic magnetic-field dependence of the Kondo effect in a one-electron DQD. Measurements of the KDC as shown in Fig. 2 but for the small magnetic-field limit. The inset and the main figure plot data for \( N=2 \) and 1, respectively. One data set (open circles) is vertically shifted for clarity. The dashed curve describes the limit \( B_{\perp} \ll B_K \) for \( N=1 \) and identical parameters as the corresponding model curve in Fig. 2. Vertical lines mark local minima of the \( N=1 \) KDC. Both datasets are taken at very similar conditions. Nevertheless, in these as in all our measurements we observe slight differences in the oscillation amplitude.
N=1 (main figure) and N=2 (inset), as plotted in Fig. 2 but at small $|B_0|<0.1$ T. All curves are symmetric with respect to the magnetic-field direction, despite a small offset of $B_{\text{offset}}=-2$ mT caused by a residual background magnetic field. As expected, the KDC for $N=2$ (inset) as well as the co-tunneling differential conductance for $N=1$ (not shown) decrease monotonically when the magnetic field increases. Surprisingly, for $N=1$ the KDC shows a nonmonotonic behavior. A pronounced local minimum at $B_1 \approx B_{\text{offset}}=0$ is followed by a quasiperiodic oscillation with minima at $|B_1| \approx 20, 30, \text{and } 42$ mT (vertical lines in Fig. 3). These oscillations quickly decay with increasing magnetic field and are convolved with the expected decrease of the KDC for $B \approx B_K$ (dashed line).

One can consider the following possible explanations for the KDC observed in a DQD for $N=1$ to be a nonmonotonic function of $B_1$: Namely, (i) the leads, (ii) nuclei spins, (iii) Aharonov-Bohm (AB) -like interferences, or (v) the alignment of energy levels of the two adjacent QDs. But all but the last of these possibilities can be ruled out.

(i) Shubnikov–de Haas oscillations in the leads cannot depend on the number of electrons. Thus, in contrast to our findings they should manifest identically in both cases for $N=1$ and 2.

(ii) Spin-orbit (SO) interaction in the leads may result in a suppression of the KDC in zero magnetic field due to spin entanglement between the electrons in the lead and the dot. The SO interaction, however, cannot explain oscillations of the KDC and a quasiperiodic peak structure. Furthermore, the SO interaction should equally affect the dot whether charged with one or two electrons. Experimentally, there is no evidence of a conductance minimum for $N=2$ (see the inset of Fig. 3). We conclude that the influence of SO interaction is negligible for the effect we observed.

(iii) In GaAs, $\sim 10^3$ nuclear spins form an internal Overhauser field $B_{\text{nuc}} \sim 10$ mT applied to the electrons on each QD. This field fluctuates on the time scale of $t_S \sim 10$ ms. In our lock-in measurements, the data are averaged over a much longer time of $\sim 300$ ms. Hence, the fluctuations of $B_{\text{nuc}}$ are unlikely to be responsible for the observed oscillations.

(iv) Interference effects in the orbital motion of an electron in a double-well potential, which determines the DQD, could lead to AB-like oscillations in the amplitude of the tunneling between the two wells. In terms of the magnetic flux, the period of the oscillation is the flux quantum $\Phi_0 = \hbar/e$. The overlap of the wave functions centered in the adjacent wells of a DQD is proportional to a relative phase shift $\langle \psi_1 | \psi_2 \rangle \propto \exp[2i(\pi B_{\text{nuc}}/\Phi_0)]$ of the classically forbidden region $S_0 \sim Ld$ (we assume a rectangular barrier of width $d$, lateral extension $L$, and height $V$ separating the two wells). Therefore, one would expect the period of the oscillation to be of the order $\Phi_0/S_0$, which is $\sim 0.5$ T for our DQD. This is far in excess of the typical quasiperiod ($\sim 10$ mT) of the observed oscillations (Fig. 3).

As to AB interferences between different tunneling paths, the area enclosed by a possible AB contour can be estimated to be $S_{AB} \sim Ld$ (or even smaller due to the serial configuration of the DQD).

We also consider the possibility of Fano-like oscillations, which would be associated with a leakage current under our gates. However, experimentally we exclude leakage currents due to several measurements (not shown here).

(v) We believe that the observed quasiperiodic oscillations can be attributed to the magnetic-field effect on the alignment of the energy levels in the two adjacent QDs. There is no reason to expect that the DQD structure is perfectly symmetric and the single electron eigenenergies $\varepsilon_{1,2}$ in the two QDs are exactly identical. The transmission through the barrier corresponding to a one-dimensional motion of an electron is determined by the overlap of the wave functions $\langle \psi_1 | \psi_2 \rangle = \sin(\kappa_1) e^{-i\kappa_1} / \kappa_1$, where $\kappa_1 = (\kappa_1 \pm \kappa_2)/2$ and $\kappa_1, \kappa_2 = \sqrt{2md^2(V-\varepsilon_{1,2})}/\hbar$. The tunneling rate reaches its maximum at resonance for $\kappa_1 = \kappa_2$.

Since the eigenenergies and, consequently, the parameters $\kappa_1, \kappa_2$ depend on the magnetic field, the latter can be used to fine-tune the tunneling rate. What is the magnetic field that can compensate a mismatch $\Delta \varepsilon = |\varepsilon_1 - \varepsilon_2|$ between the ground-state eigenenergies of the two wells? Using the 1D Schrödinger equation for a rectangular (or parabolic) double-well potential, one obtains $\hbar \omega_c = \sqrt{|\varepsilon_1 - \varepsilon_2|} \Delta \varepsilon / W$, where $W$ is the energy difference between the two local minima of the double-well potential and $\omega_c = |eB/m|$ is the cyclotron frequency.

At $B_0 = 0$, the energy mismatch $\Delta \varepsilon$ is finite. It takes about $B_0 = \pm 12$ mT to align the ground states, which corresponds to the first KDC maximum. The suppression of the mismatch by the magnetic field explains the pronounced minimum at $B_1 = 0$. This behavior is obviously symmetric with respect to the sign of the magnetic field. Note that the characteristic magnetic field $B_0$ can be very small due to the factor $\sqrt{|\varepsilon_1 - \varepsilon_2|}$, roughly estimated to be $\sim 10^{-3}$ for our setup. The interdot tunneling rate is unaffected by thermal line broadening as long as it corresponds to low-frequency noise allowing adiabatic alignment of the energy levels in both QDs.

The remaining KDC maxima at slightly larger magnetic fields probably correspond to alignments of excited energy states in the two QDs. This implies the importance of cotunneling processes, which are indeed strong [compare Fig. 1(c)]. Moreover, in order to explain the observed quasiperiodic magnetic-field dependence, the level structures in the two QDs should differ due to some anisotropy. From the number of observed KDC maxima, we conclude that at least three excited states are involved in the cotunneling.

Our model is consistent with the missing KDC oscillations for the doubly occupied DQD ($N=2$). Indeed, for $N=2$ and a symmetric charge distribution with one electron in each dot, transport is determined by the singlet and triplet states. The symmetric charge distribution allows enhanced elastic cotunneling, decreasing the dependence on the misalignment of the single dot ground states.

In conclusion, we presented here measurements of the Kondo effect on a DQD charged by only one or two electrons. We demonstrate control of the resonant tunneling in the one-electron case by means of a magnetic field that appears to be surprisingly small. A nonmonotonic magnetic-field dependence of the KDC is attributed to the anisotropy of the DQD. The magnetic field fine-tunes the alignment of energy levels in the adjacent QDs, modifying the interdot tunnel splitting. Hence, the magnetic field provides an ex-
extremely sensitive tool to detect and control the anisotropy of a single-electron DQD.

Our double dot with strong coupling to the leads is not a perfect system for a qubit. However, the influence of a very small misalignment of the single dot energy levels onto the tunnel probability of the electron will remain even for a double dot weakly coupled to the leads, which can be used, e.g., as a charge qubit. The observed variations of the interdot tunnel splitting at very small magnetic fields have to be taken into account for the design of semiconductor nanodevices in the field of quantum information processing.

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